

Statistical Potentials in Rosetta

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OUR NEW JUSTICE



Confirmed 68-31

Statistical Potentials in Rosetta

- Ramachandran term

(coil residues)

$$p(\phi, \psi | Res)$$

- Rotamer term

(all residues)

$$p(r | \phi, \psi, Res)$$

- Design term

(all residues)

$$p(Res | \phi, \psi)$$

- Hydrogen bond, other terms...

Important to be smooth, differentiable (ϕ, ψ) $d \log p / d\phi$

Based on accurate input data

What input data sets? (all sec. str, coil, turns?)

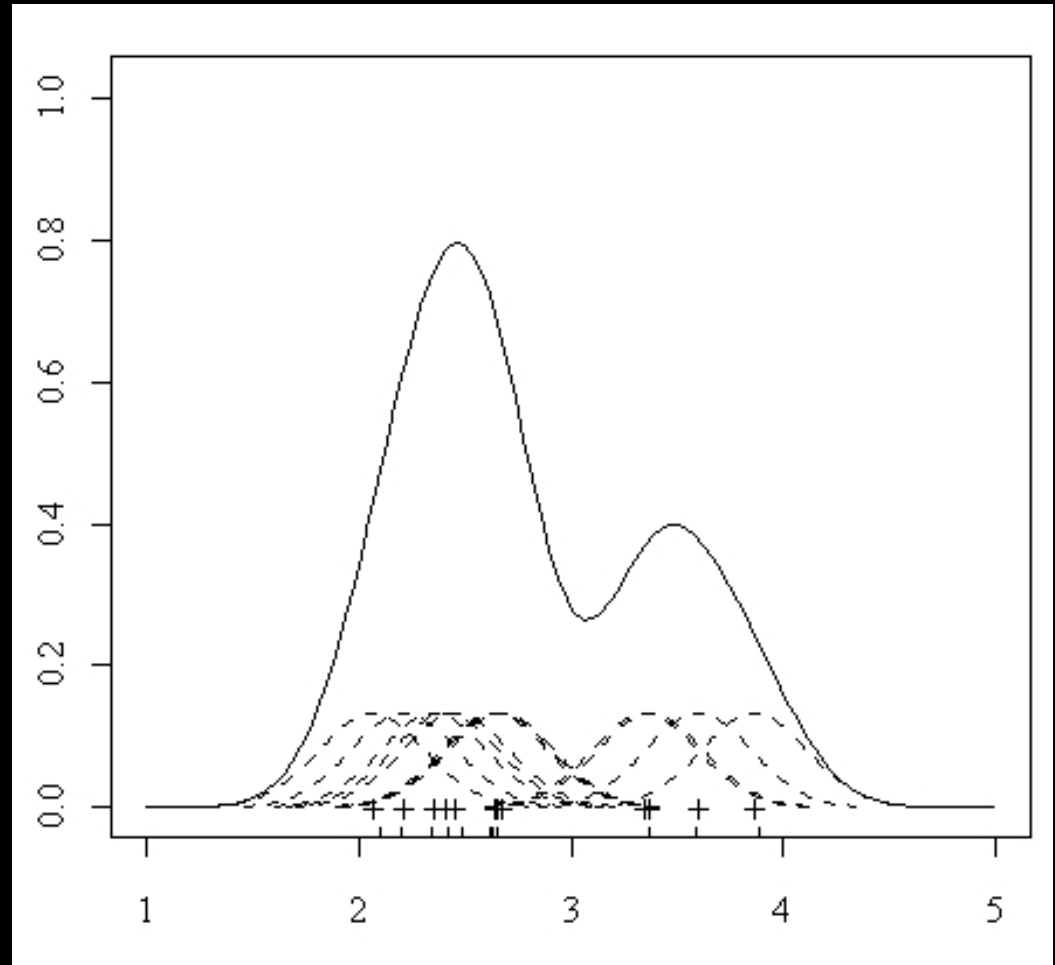
Non-parametric statistics

Kernel density estimates

Assign a function (kernel) to every data point to spread out or smooth the data. At each “query point” (e.g. on a regular grid), add the value of all the kernels.

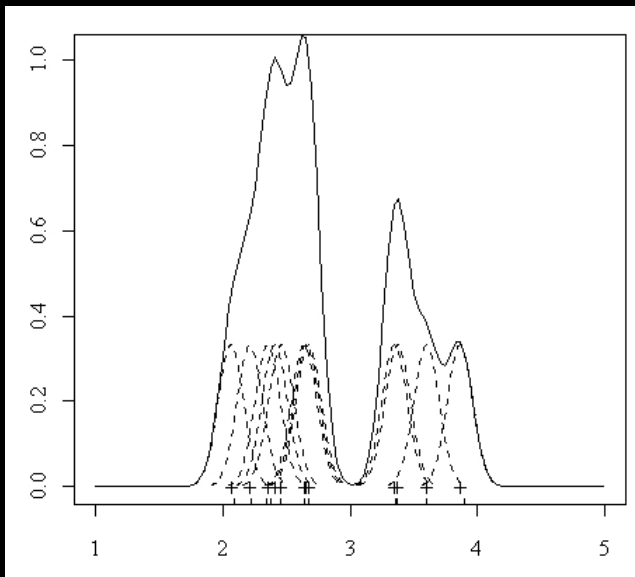
$$\hat{p}(x) = \frac{1}{nh} \sum_{k=1}^n K\left(\frac{x - x_i}{h}\right)$$

$$\int_U K(u) du = 1$$

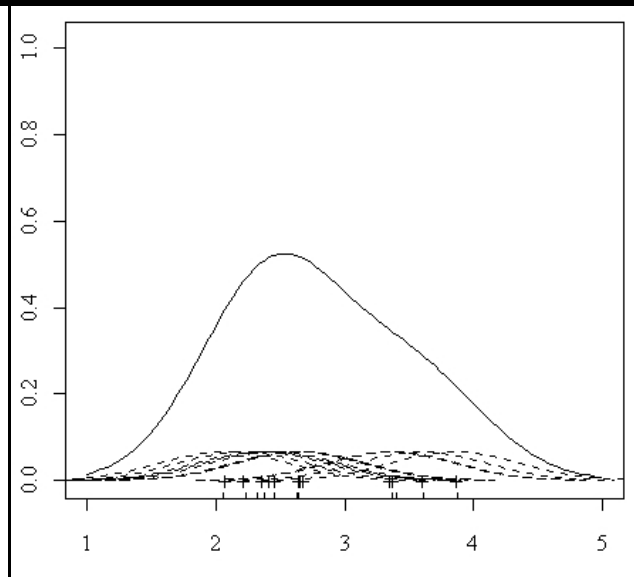


Kernel width

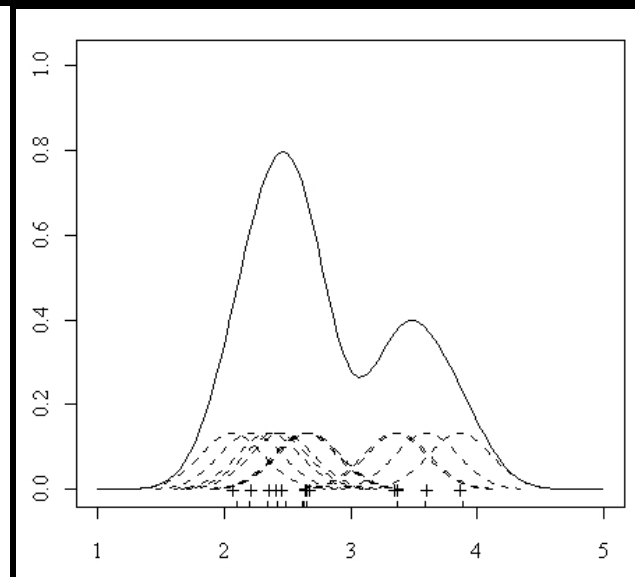
Undersmoothed



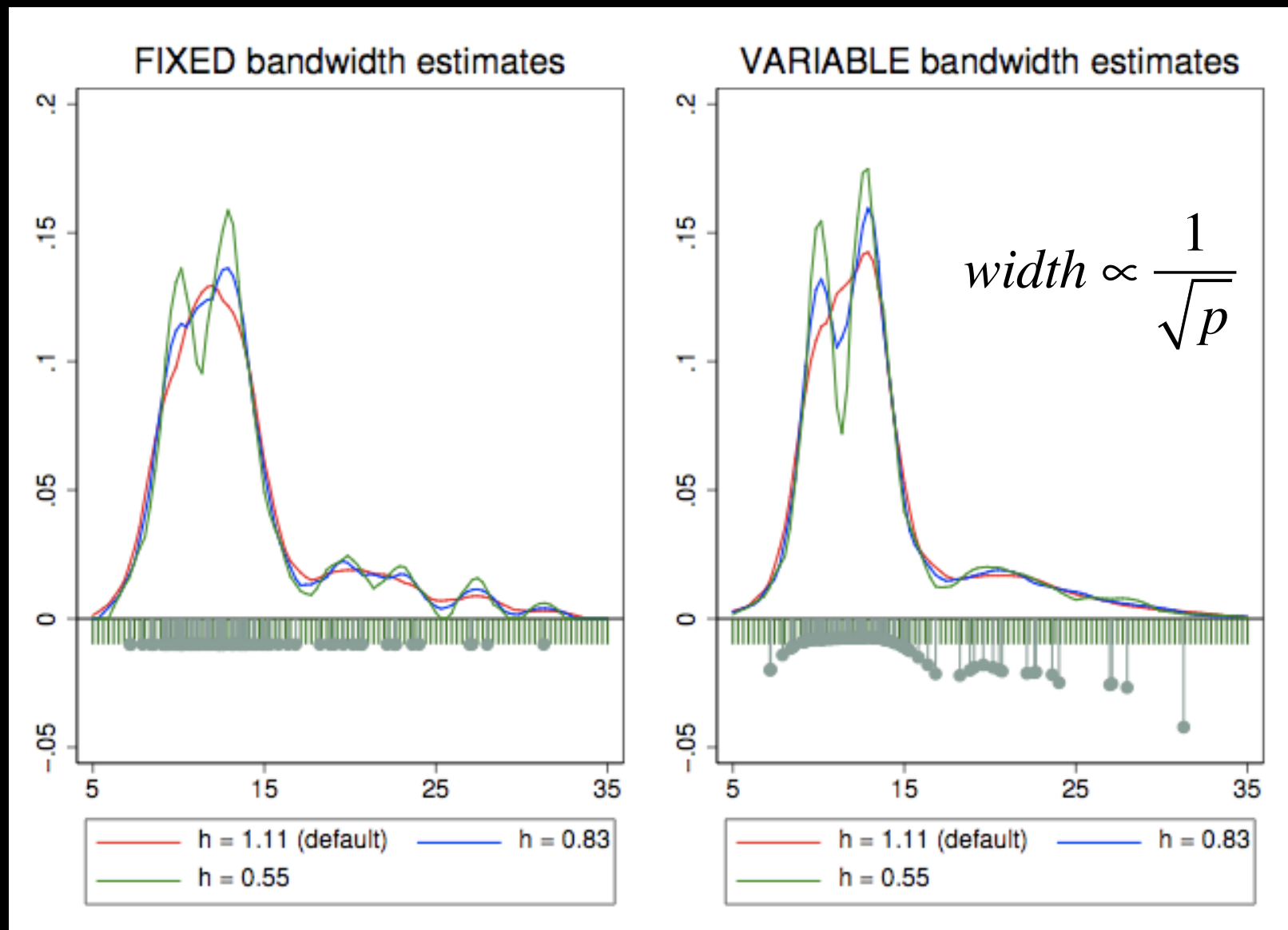
Oversmoothed



Optimally smoothed



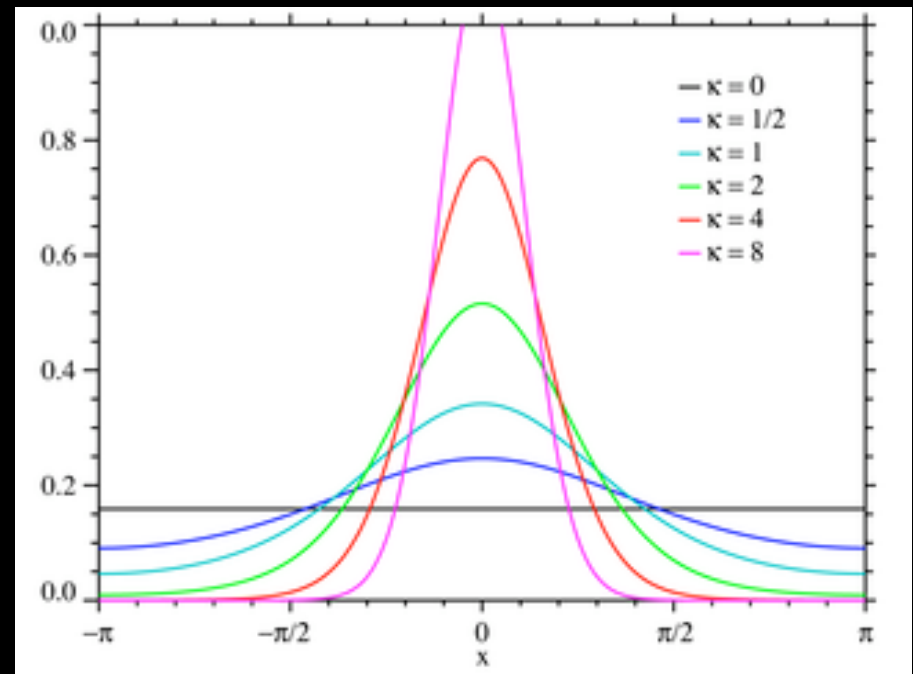
Adaptive kernel density estimates



Directional statistics

Von Mises Probability Distributions

$$p(\theta) = \frac{\exp(\kappa \cos(\theta - \theta_0))}{2\pi I_0(\kappa)}$$



(wikipedia page on Von Mises distns)

For large kappa, very close to normal distributions

Using Von Mises Distributions for Adaptive Kernel Density Estimates of Angular Data

$$\hat{p}(x) = \frac{1}{n} \sum_{i=1}^n \frac{1}{2\pi I_0(\kappa/h_i)} \exp\left(\frac{\kappa}{h_i} \cos(x - x_i)\right)$$

Ramachandran PDF

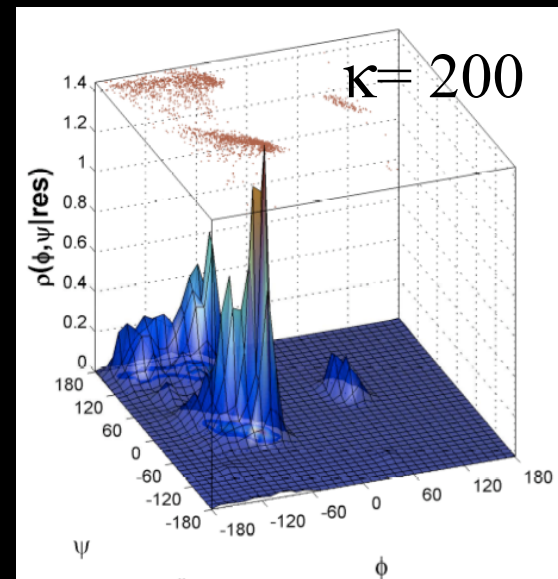
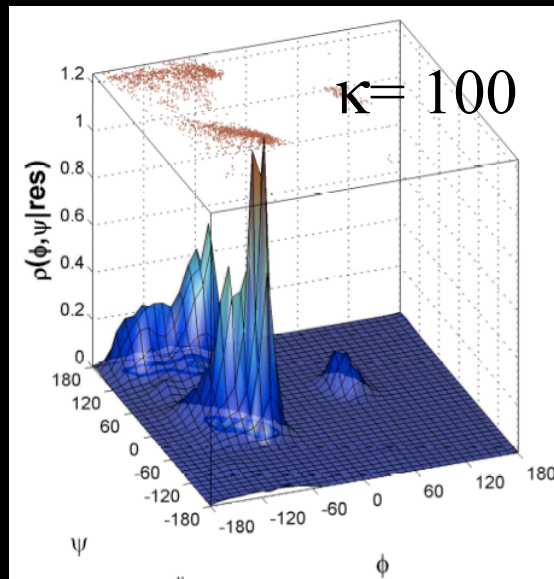
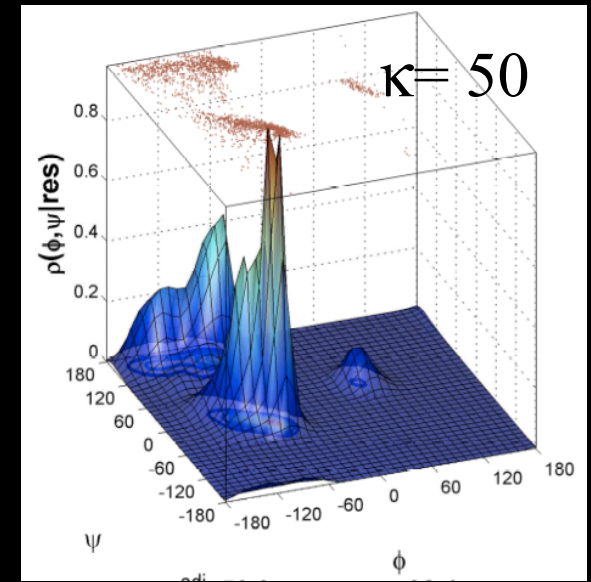
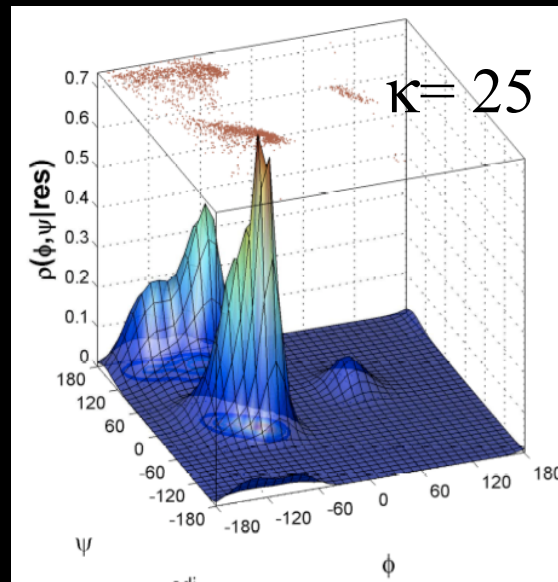
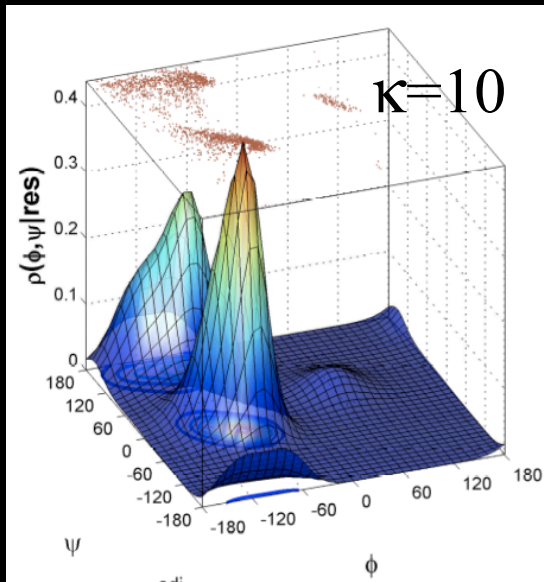
$$p(\phi, \psi | Res) = \frac{1}{4\pi^2 N} \sum_{i=1}^N \frac{1}{(I_0(\kappa / \lambda_i))^2} \exp\left(\frac{\kappa}{\lambda_i} (\cos(\phi_i - \phi) + \cos(\psi_i - \psi))\right)$$

$$\lambda_i = \sqrt{\frac{\prod_i \hat{f}(\phi_i, \psi_i)}{\hat{f}(\phi_i, \psi_i)}}$$

κ becomes
geometric mean of
kernel widths

Kernel widths from pilot density estimate from non-adaptive KDE

Rama potential: kernel widths



Gln

Ramachandran Data

10495 Loops len $\geq$ 8

Turn 47%

Coil 36%

310H 13%

Bridge 4%

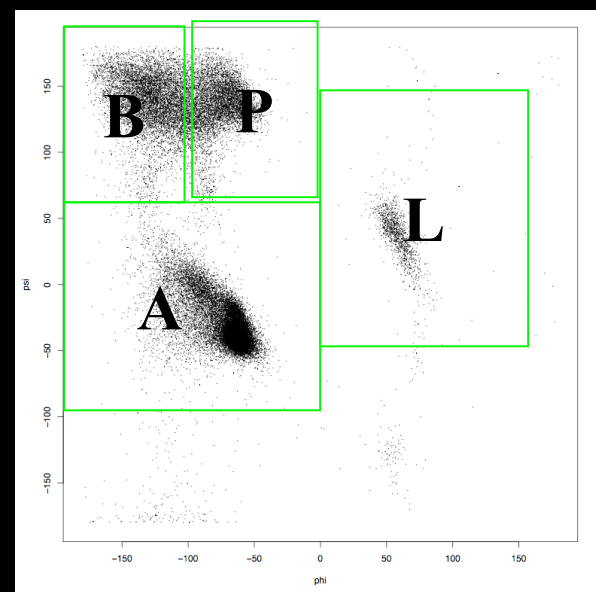
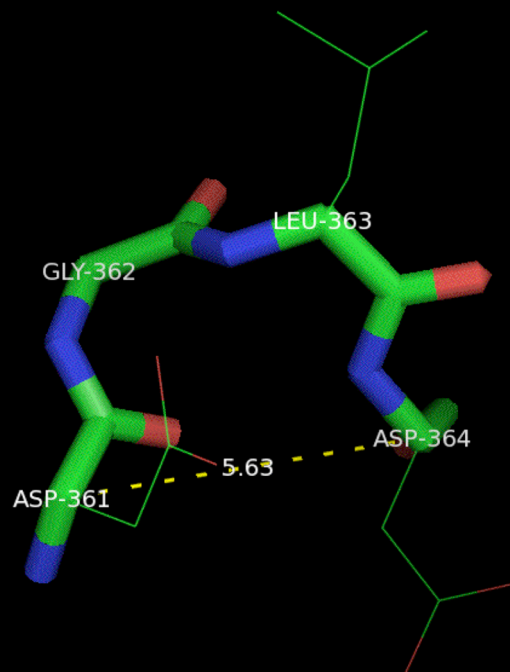
Loop Turn Coil 310H

A 38% 42% 18% 96%

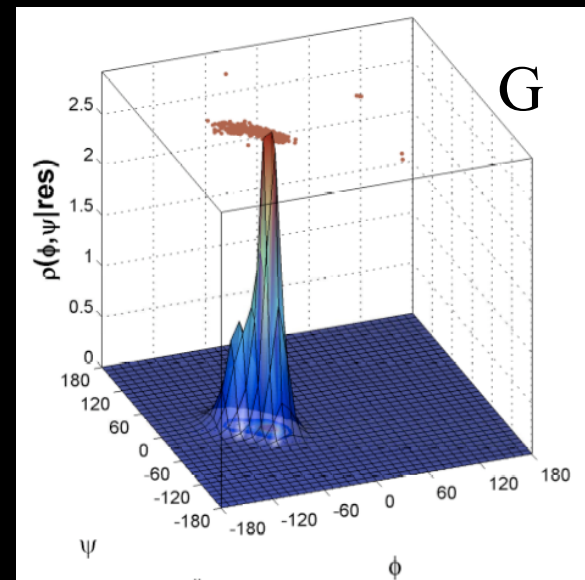
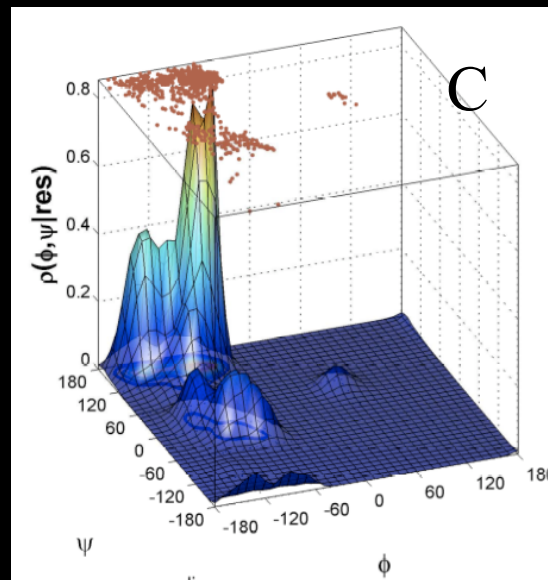
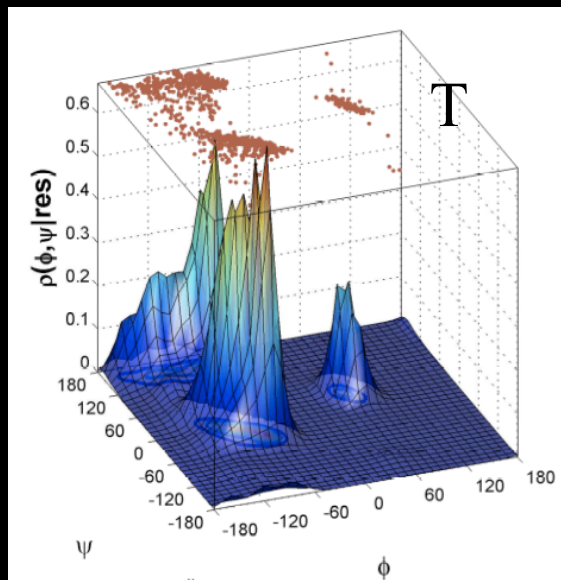
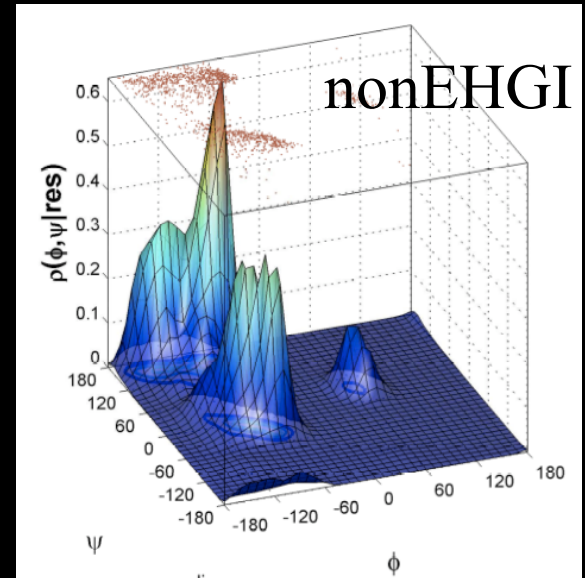
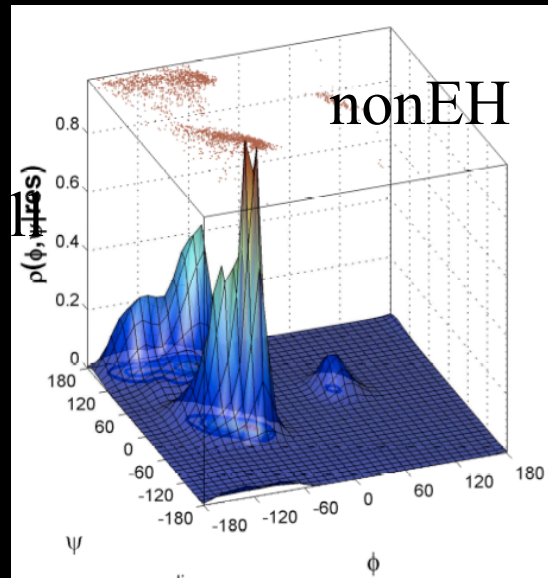
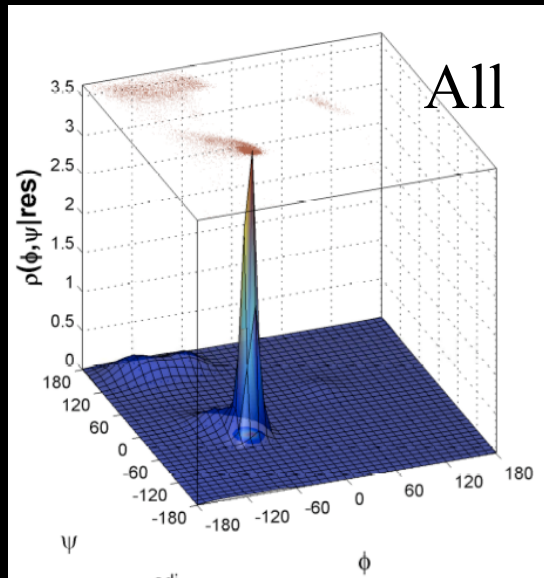
B 23% 19% 32% 0%

P 28% 25% 41% 0%

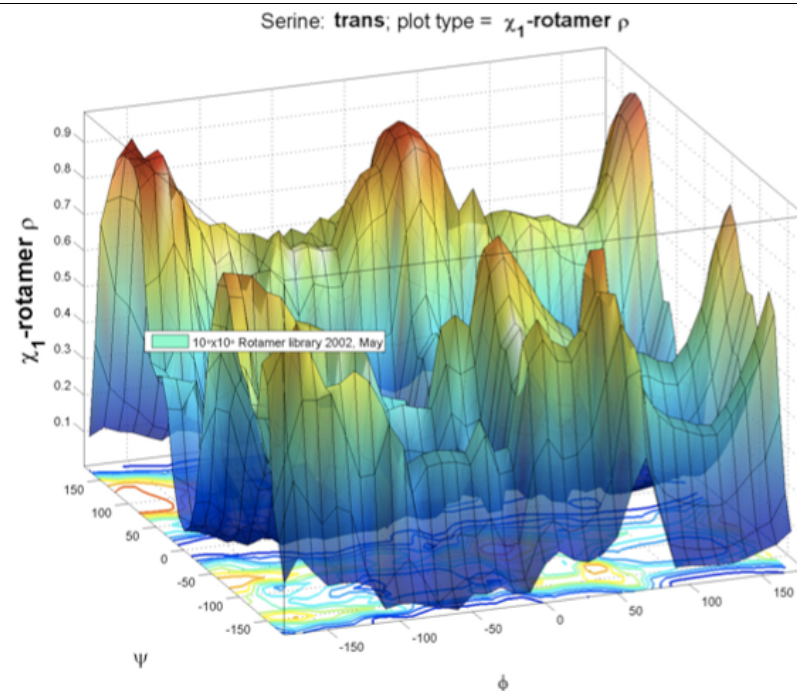
L 10% 13% 9% 3%



Rama potential: input sets



2002 Library



850 proteins

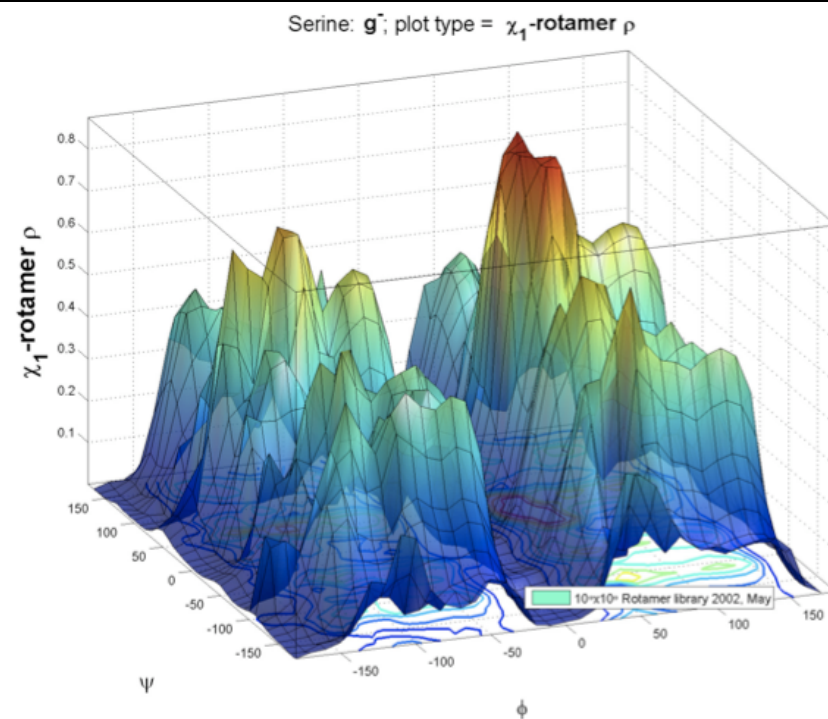
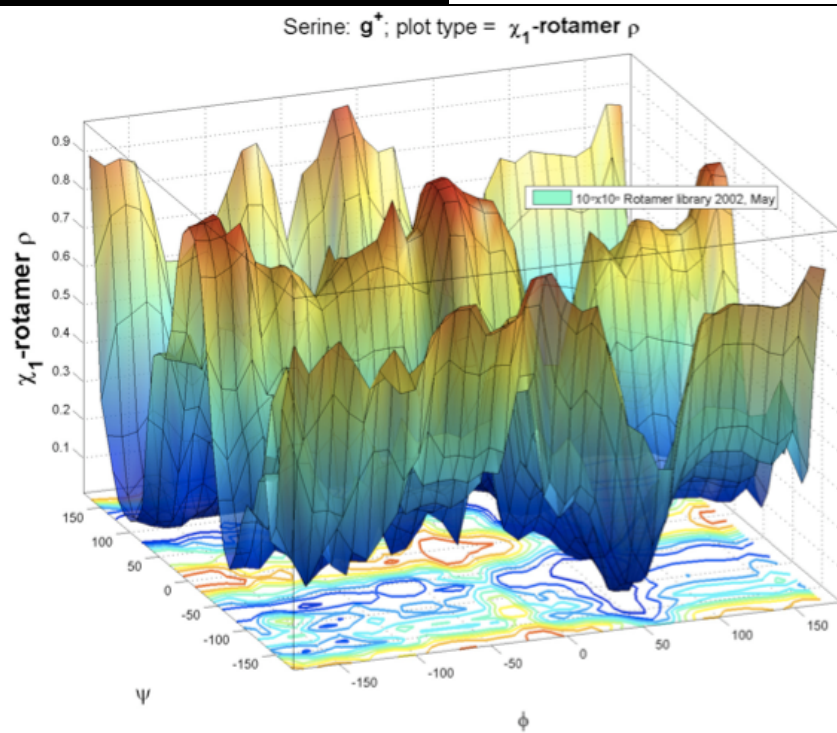
$\leq 1.7\text{\AA}$

$\leq 50\%$ id

Asn/Gln/His
flips

B-factor < 40

No contacts

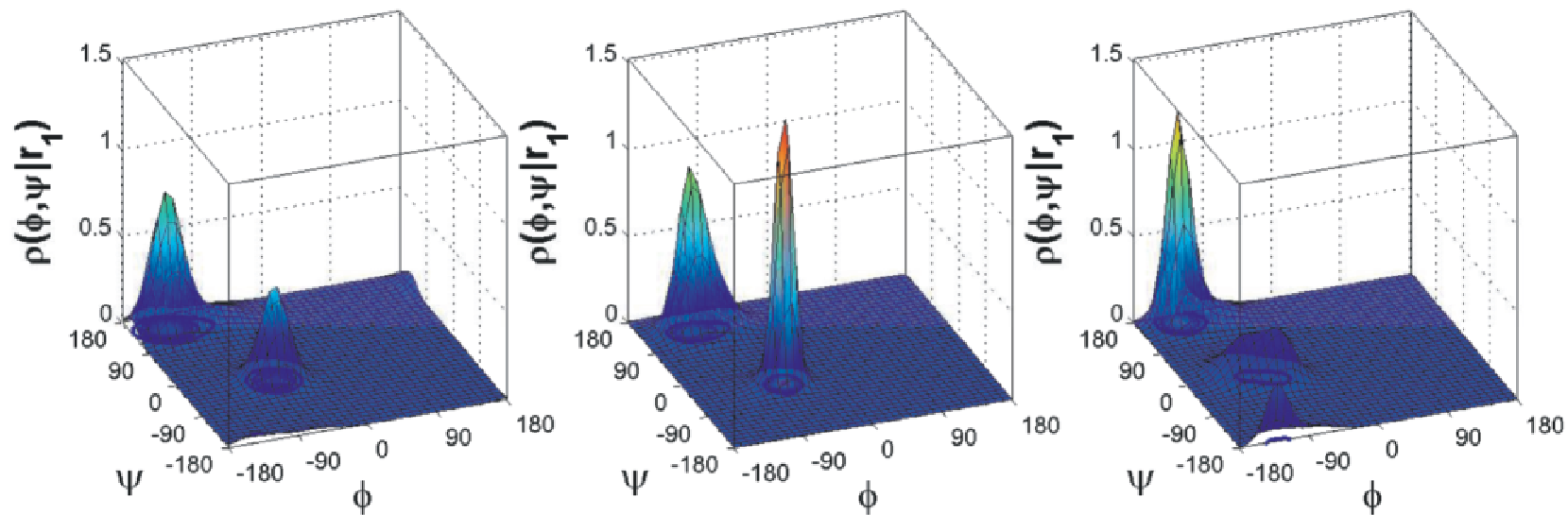


Adaptive kernel density estimates Ramachandran distribution for each rotamer of Valine

g⁺

trans

g⁺



$$p(\phi, \psi | r) = \frac{1}{4\pi^2 N_r} \sum_{i=1}^{N_r} \frac{1}{(I_0(\kappa/\lambda_i))^2} \exp\left(\frac{\kappa}{\lambda_i} (\cos(\phi_i - \phi) + \cos(\psi_i - \psi))\right)$$

Bayes' rule

We can get $p(\phi, \psi | r)$. How do we get $p(r | \phi, \psi)$?

Invert using Bayes' rule:

$$p(A, B) = p(A|B)p(B) = p(B|A)p(A)$$

$$p(A|B) = \frac{p(B|A)p(A)}{p(B)}$$

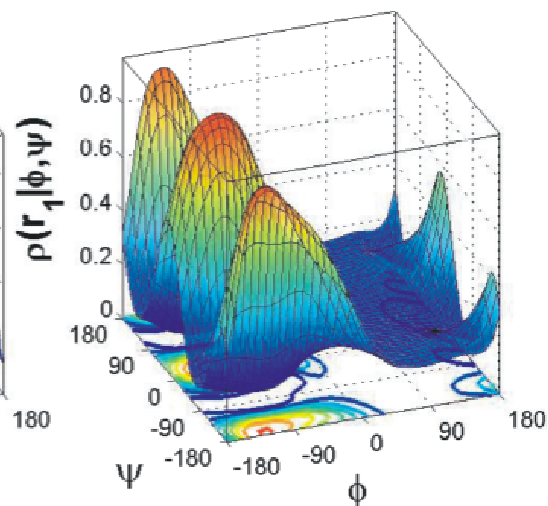
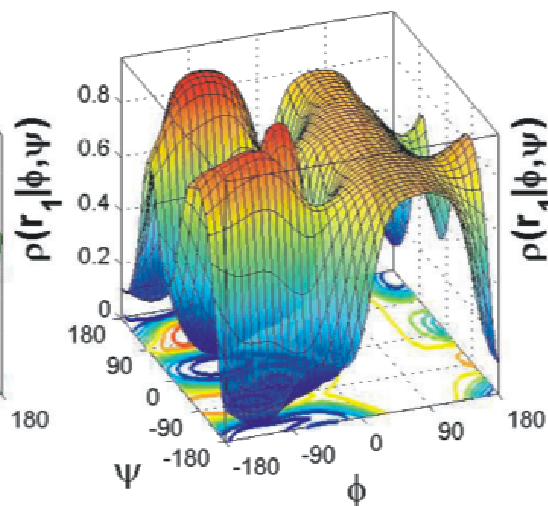
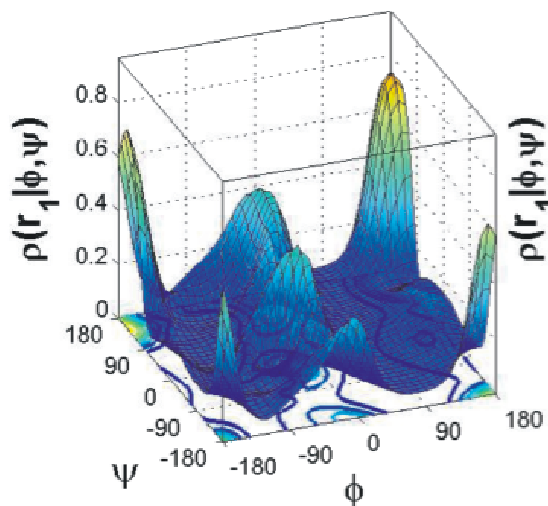
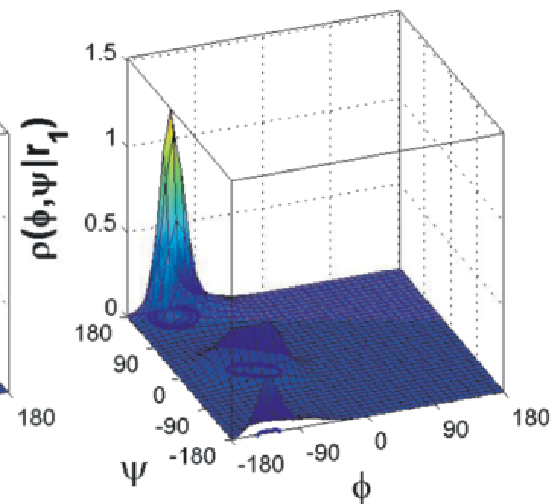
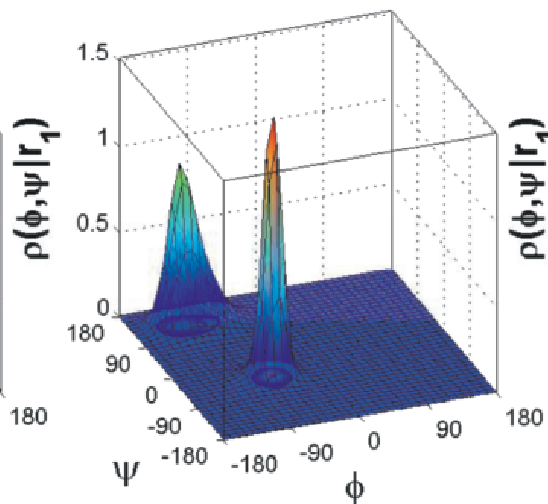
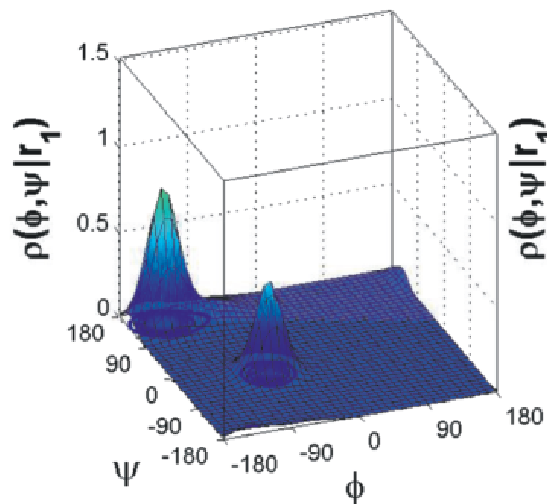
$$p(r | \phi, \psi) = \frac{p(\phi, \psi | r) p(r)}{\sum_{r'} p(\phi, \psi | r') p(r')}$$

Valine

g^+

trans

g^-



Kernel widths

Cross validation of log likelihood

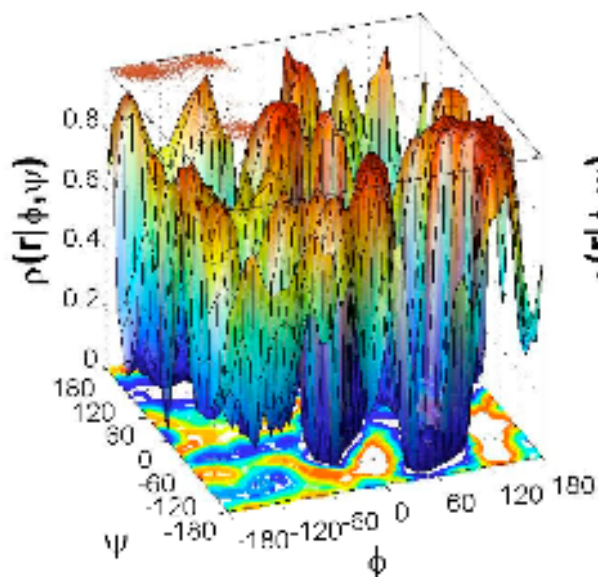
In ϕ, ψ space,
rotamer-dep

$$L(r; \kappa) = \prod_i p(\phi_i, \psi_i | r)$$
$$\log L(r; \kappa) = \sum_i \ln p(\phi_i, \psi_i | r)$$

Maximize $\log L$ for
each rotamer as a
function of κ by
calculating p on 90%
of data and evaluating
 L on 10%

In ϕ, ψ space,
rotamer-
indep

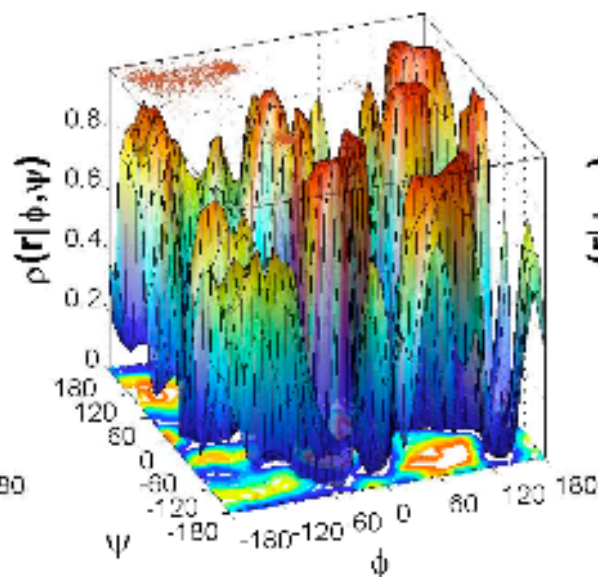
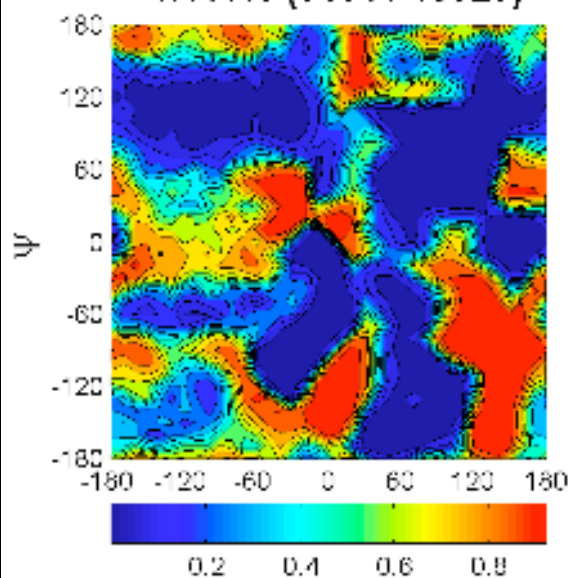
$$L(\kappa) = \prod_i p(\phi_i, \psi_i)$$
$$\log L(\kappa) = \sum_i \ln p(\phi_i, \psi_i)$$



$\kappa^{\text{optCV}} = 468.9$ [95%-wind=10.6°]

$\langle g^+ \rangle :$

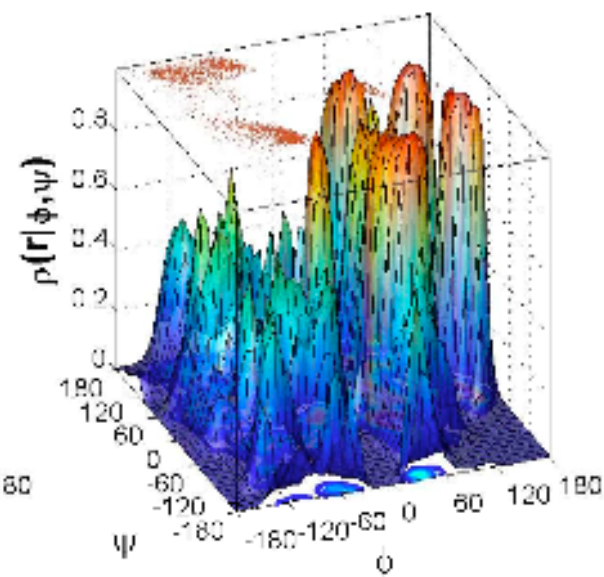
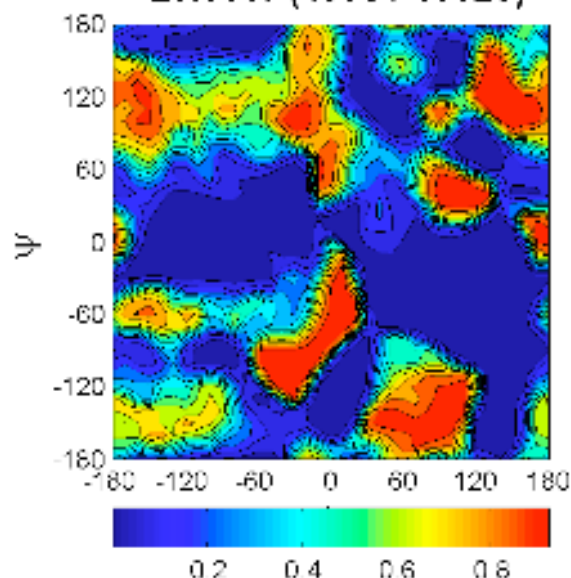
47.41% (9161 / 19323)



$\kappa^{\text{optCV}} = 283.9$ [95%-wind=13.6°]

$\langle t \rangle :$

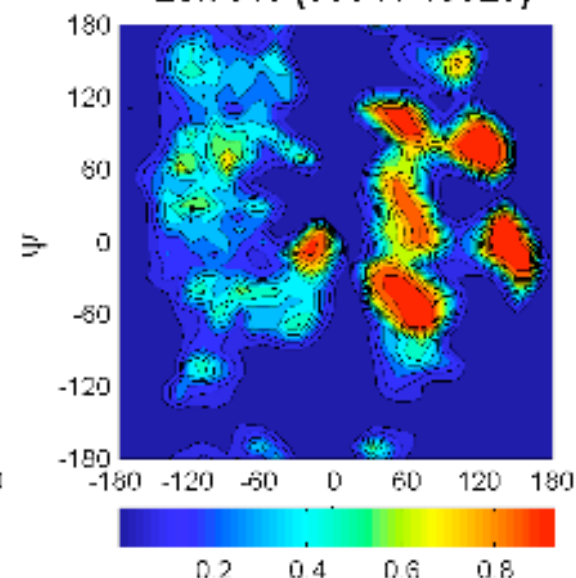
23.80% (4598 / 19323)



$\kappa^{\text{optCV}} = 408.6$ [95%-wind=11.3°]

$\langle g^+ \rangle :$

28.79% (5564 / 19323)



Correct way

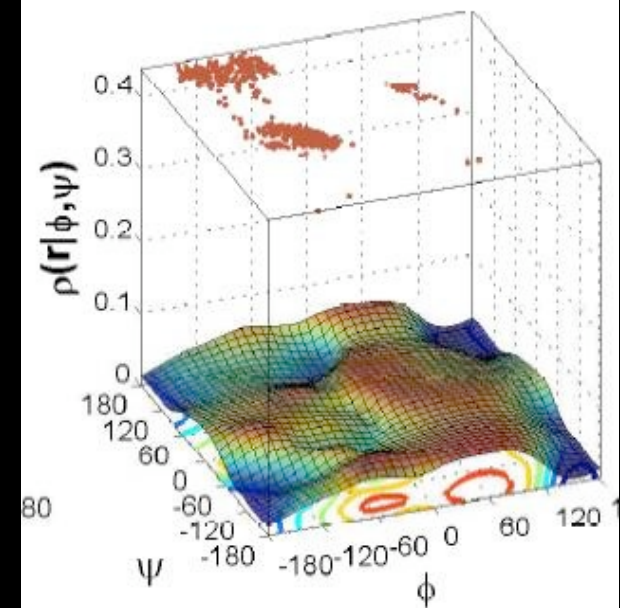
In r space

$$L(\kappa) = \prod_i p(r|\phi_i, \psi_i)$$

$$\log L(\kappa) = \sum_i \log p(r|\phi_i, \psi_i)$$

Same $(\phi, \psi) \rightarrow$ same κ

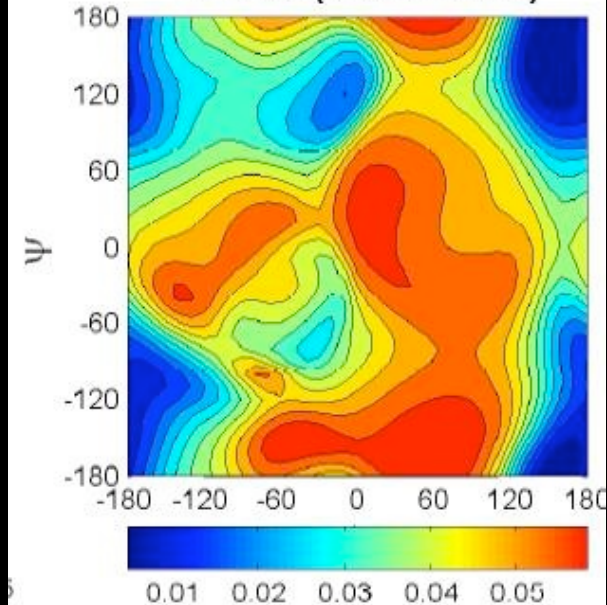
$$\lambda_i = \left(\frac{\left(\prod_{j=1, N} \hat{f}(\phi_j, \psi_j) \right)^{\frac{1}{N}}}{\hat{f}(\phi_i, \psi_i)} \right)^{\frac{1}{2}}$$



$\kappa^{\text{optCV}} = 12.7$ [95%-wind $\approx 64.3^\circ$]

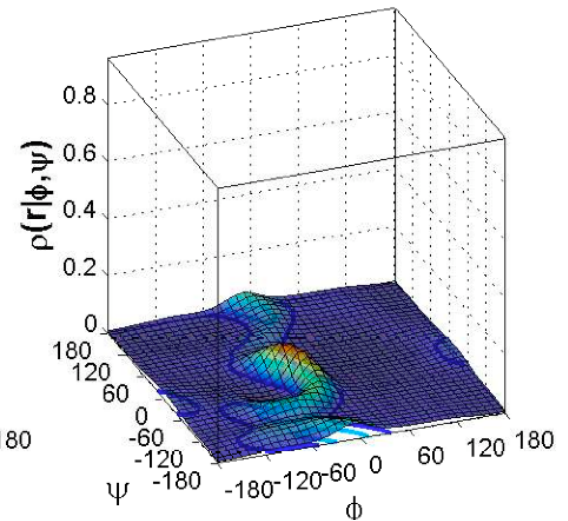
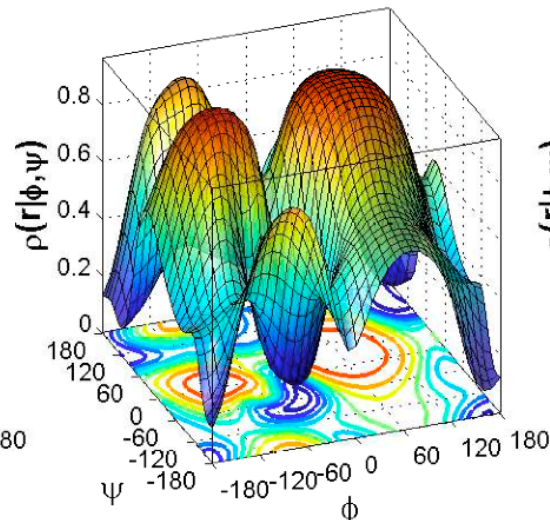
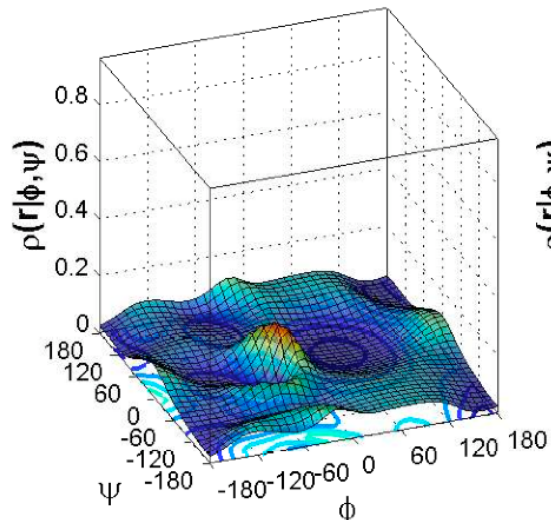
$\langle g^- t g^+ t \rangle :$

4.12% (715 / 17351)

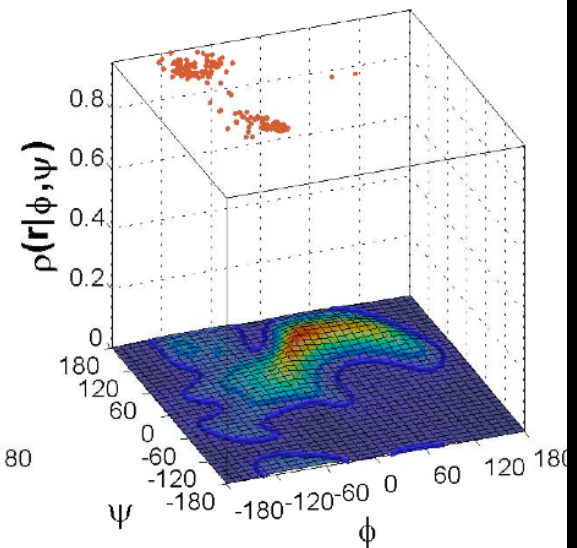
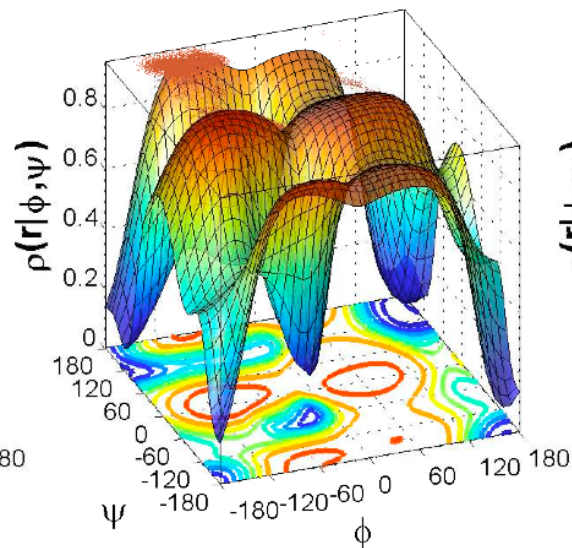
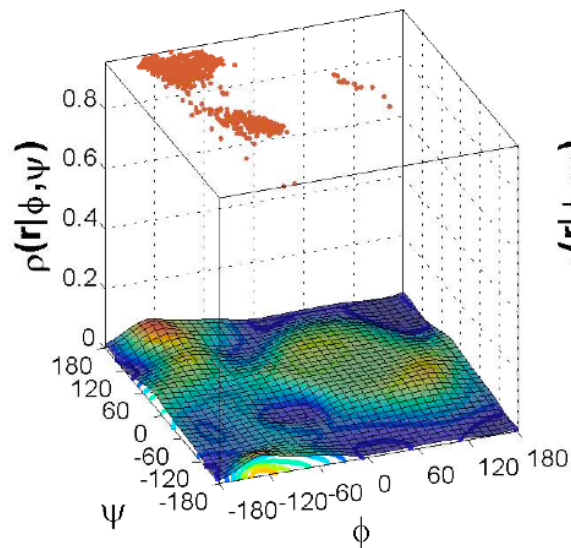


July
2008

LEU $\kappa_1^m = 25$ [$2\sigma \approx 22.9^\circ$], $\alpha_0 = 0.5$; dataPoints, adap



Feb
2009



$\kappa^{\text{optCV}} = 25.3$ [95%-wind $\approx 45.5^\circ$]

$\langle g^- g^+ \rangle :$

3.21% (954 / 29742)

$\kappa^{\text{optCV}} = 25.3$ [95%-wind $\approx 45.5^\circ$]

$\langle g^- t \rangle :$

62.30% (18529 / 29742)

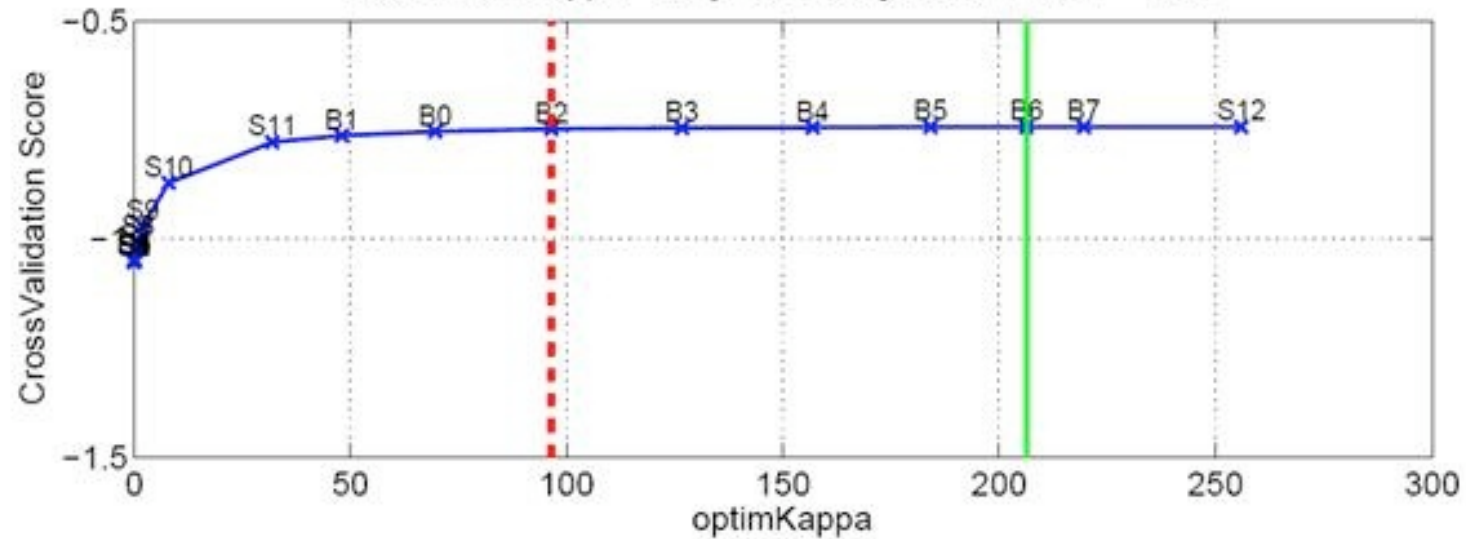
$\kappa^{\text{optCV}} = 25.3$ [95%-wind $\approx 45.5^\circ$]

$\langle g^- g^- \rangle :$

0.65% (192 / 29742)

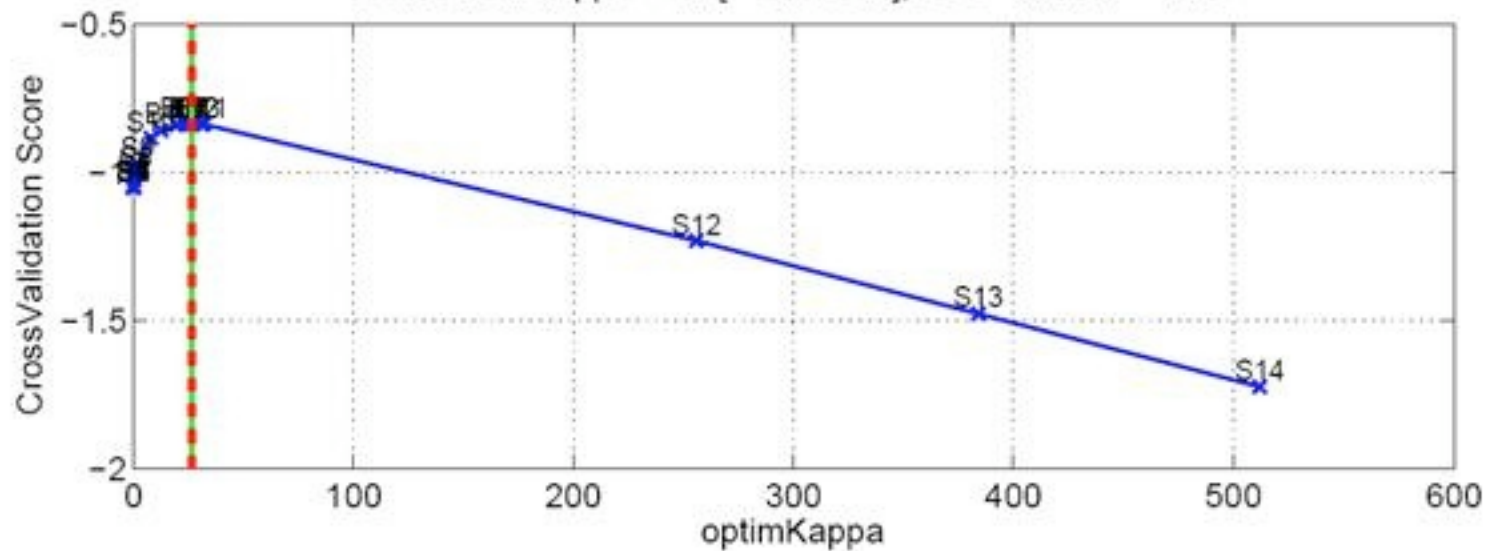
Dim2 : DensEstim, phipsi :: <all|r-Space> | data points # = 19323

EstBest CV kappa = 97 [-0.74875], 95%-window = 23.3°

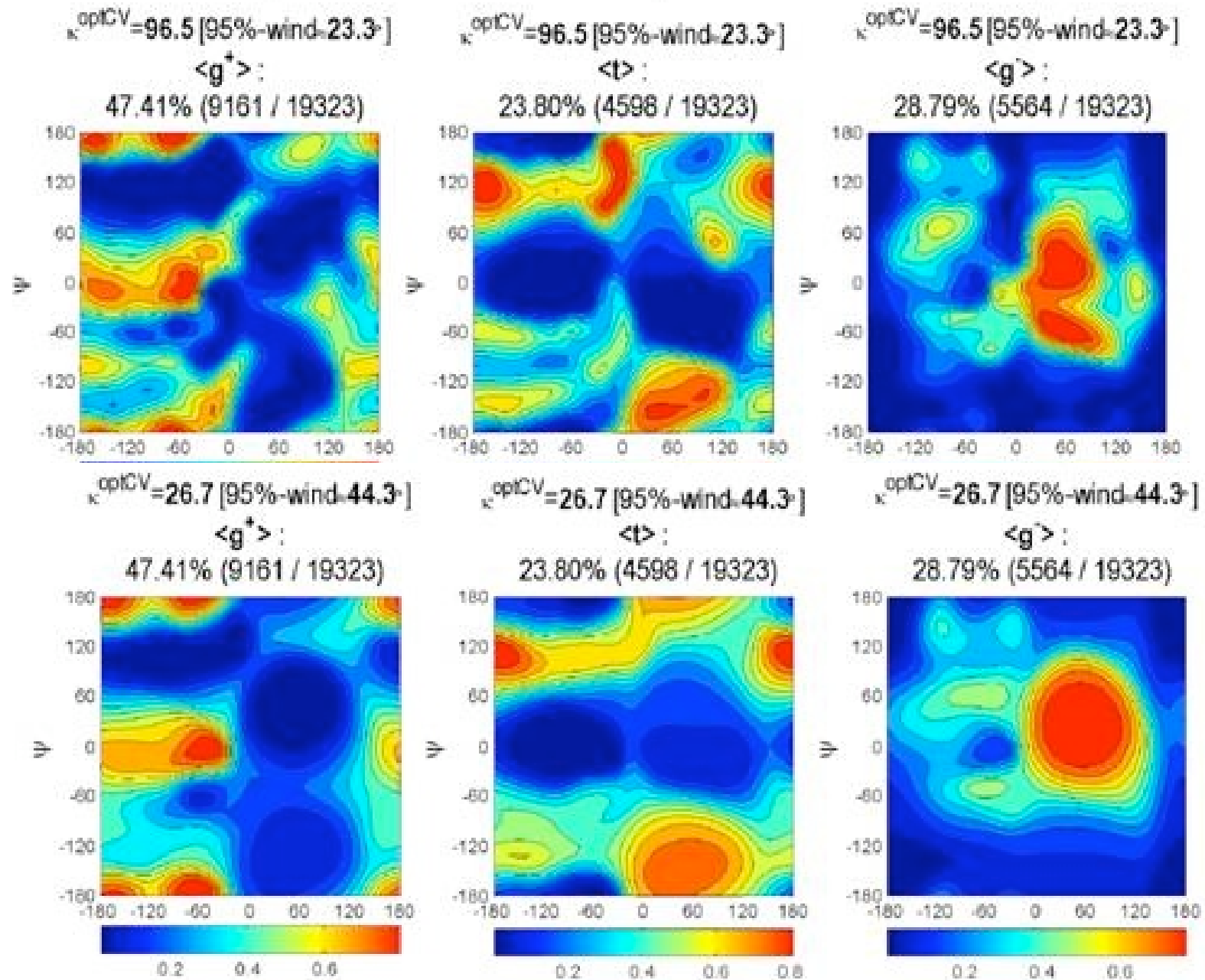


Dim2 : DensEstim, phipsi :: <all|r-Space> | data points # = 19323

EstBest CV kappa = 27 [-0.83787], 95%-window = 44.3°



No
prior



With
Prior

June
2009

Design term

Current

$$p(Res|\phi, \psi) = \frac{N(Res|\phi \pm \Delta, \psi \pm \Delta)}{N(\phi \pm \Delta, \psi \pm \Delta)}$$

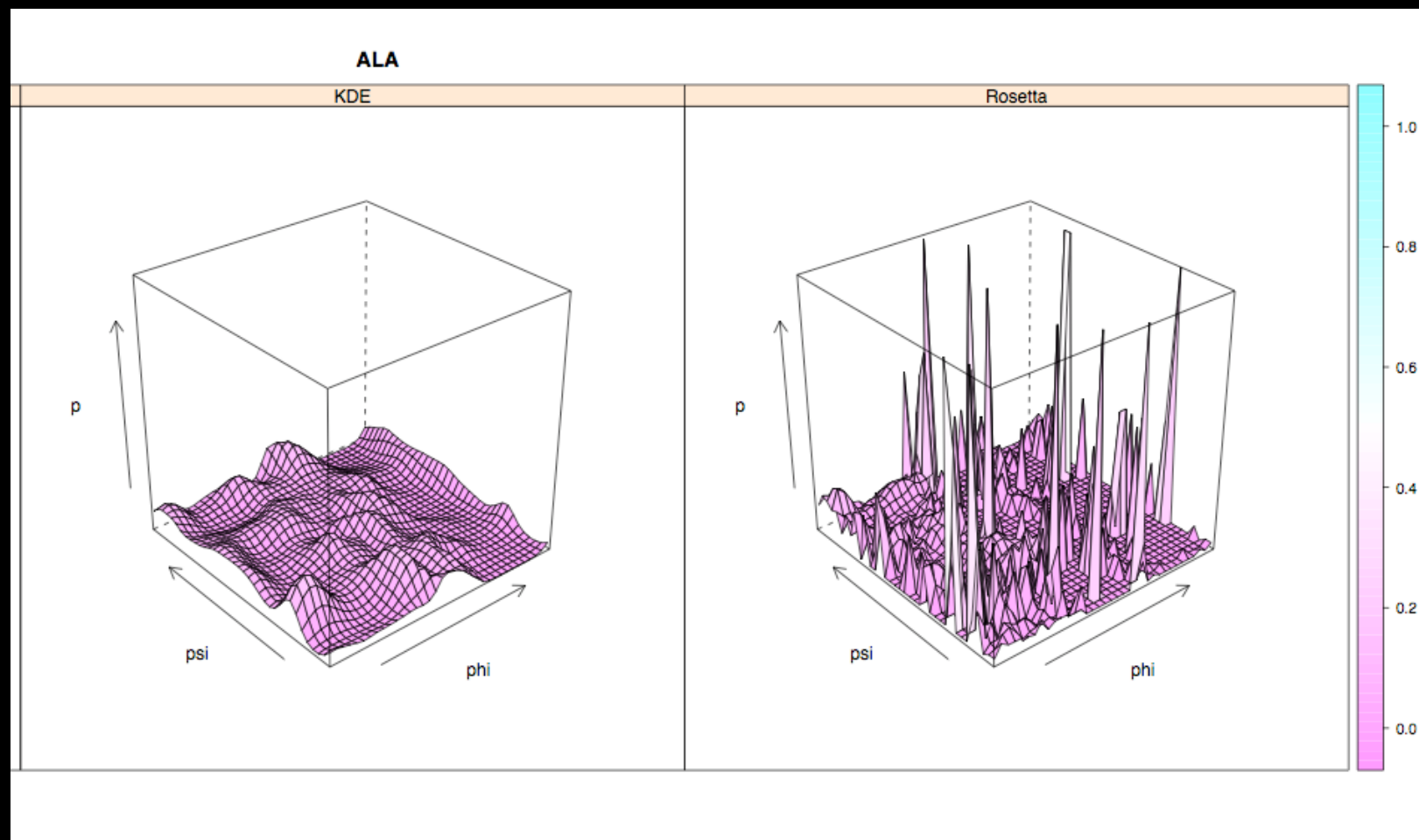
Proposed

$$p(Res|\phi, \psi) = \frac{p(\phi, \psi|Res) p(Res)}{\sum_i p(\phi, \psi|Res_i) p(Res_i)}$$

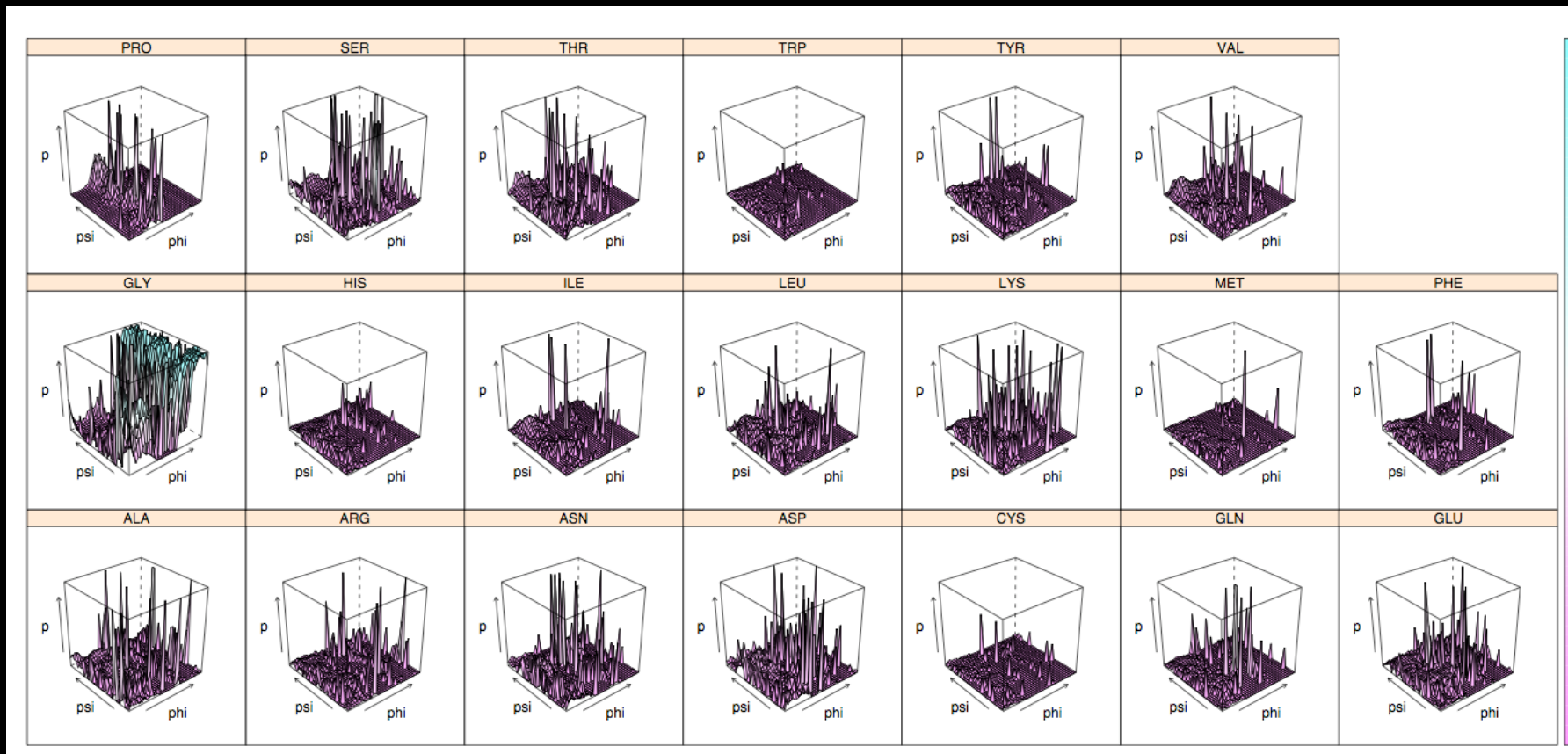
$$p(\phi, \psi|Res)$$

comes from kernel density estimates

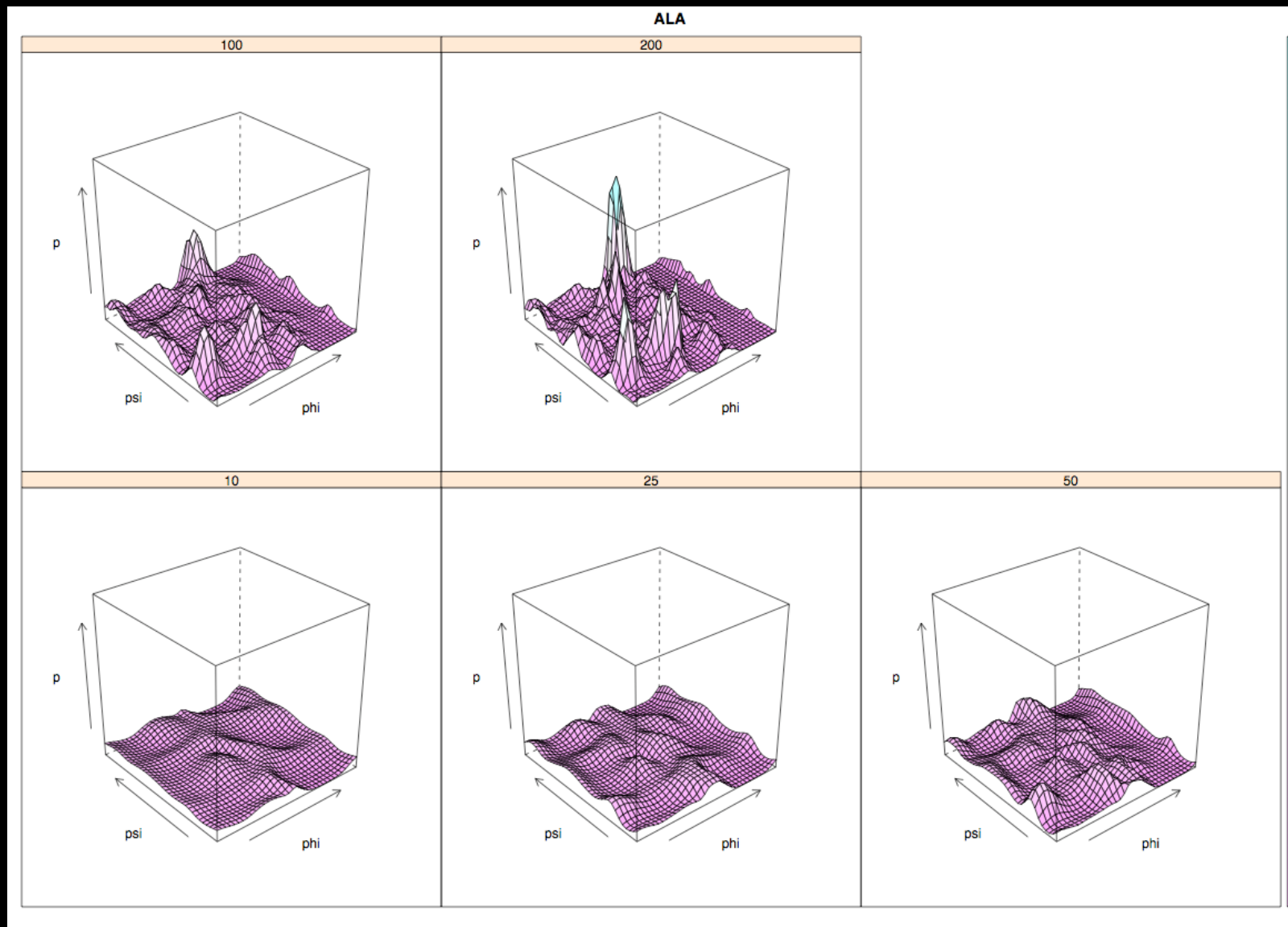
Propensities



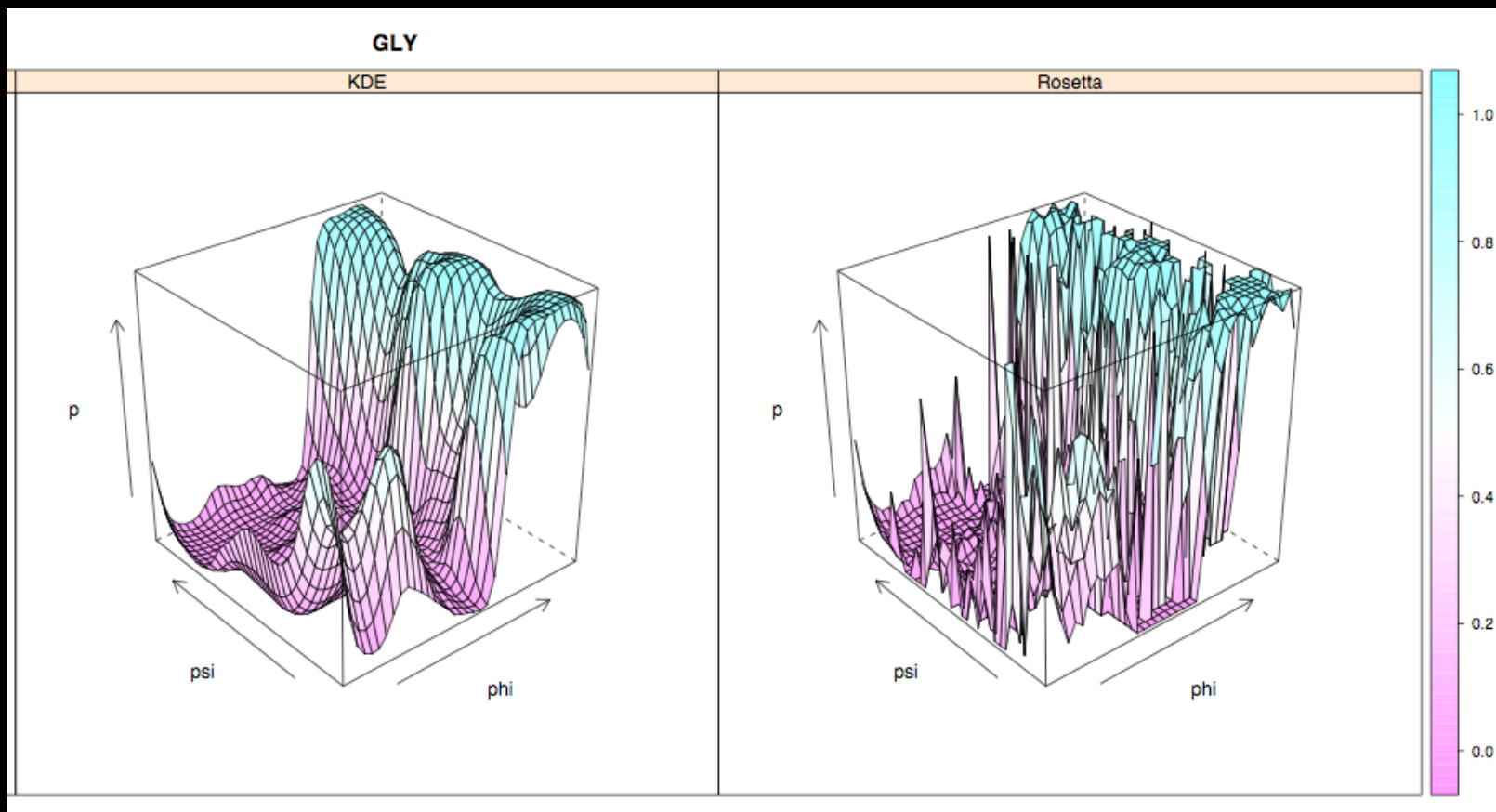
Rosetta's current design term



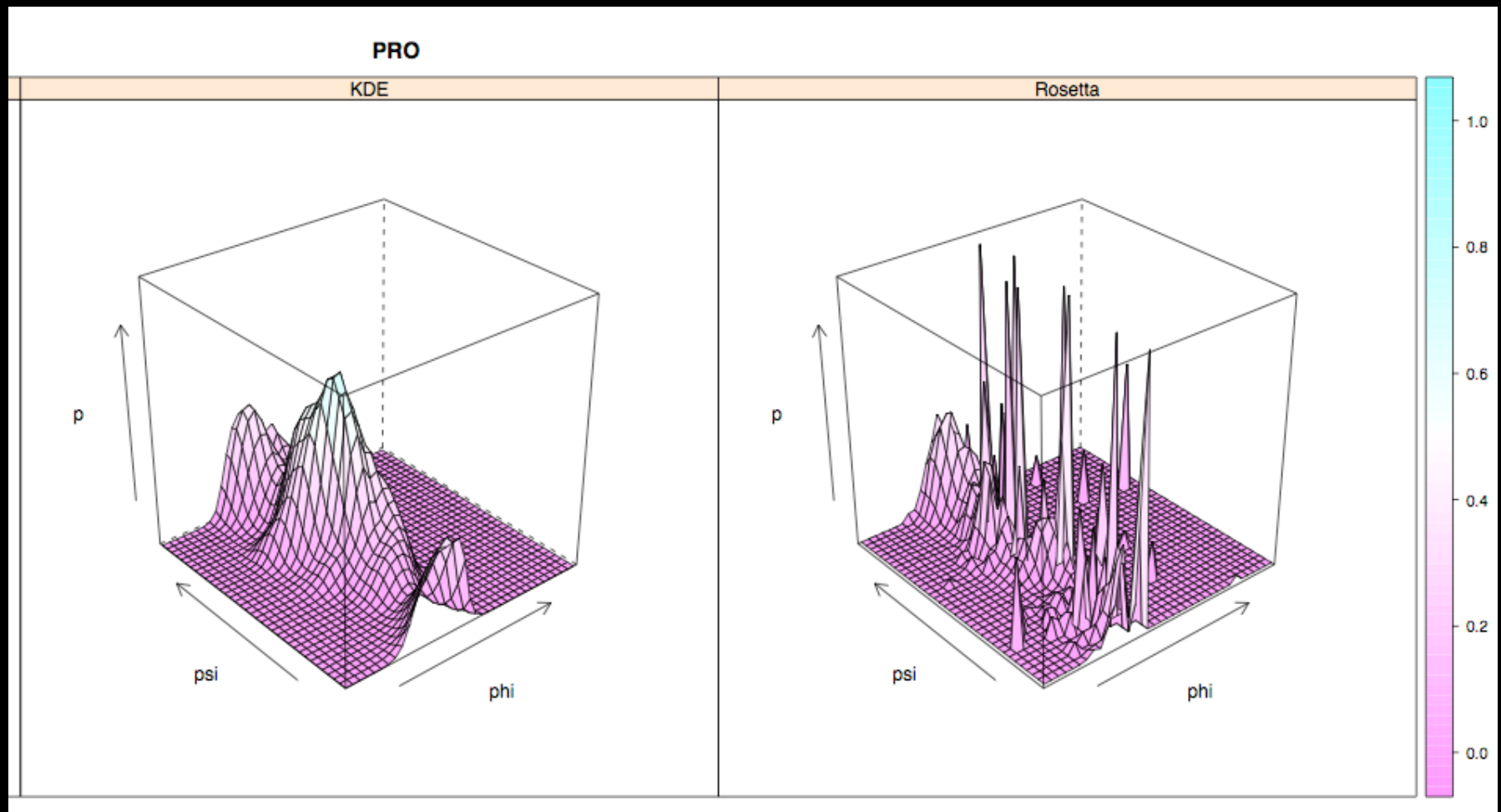
Kappa



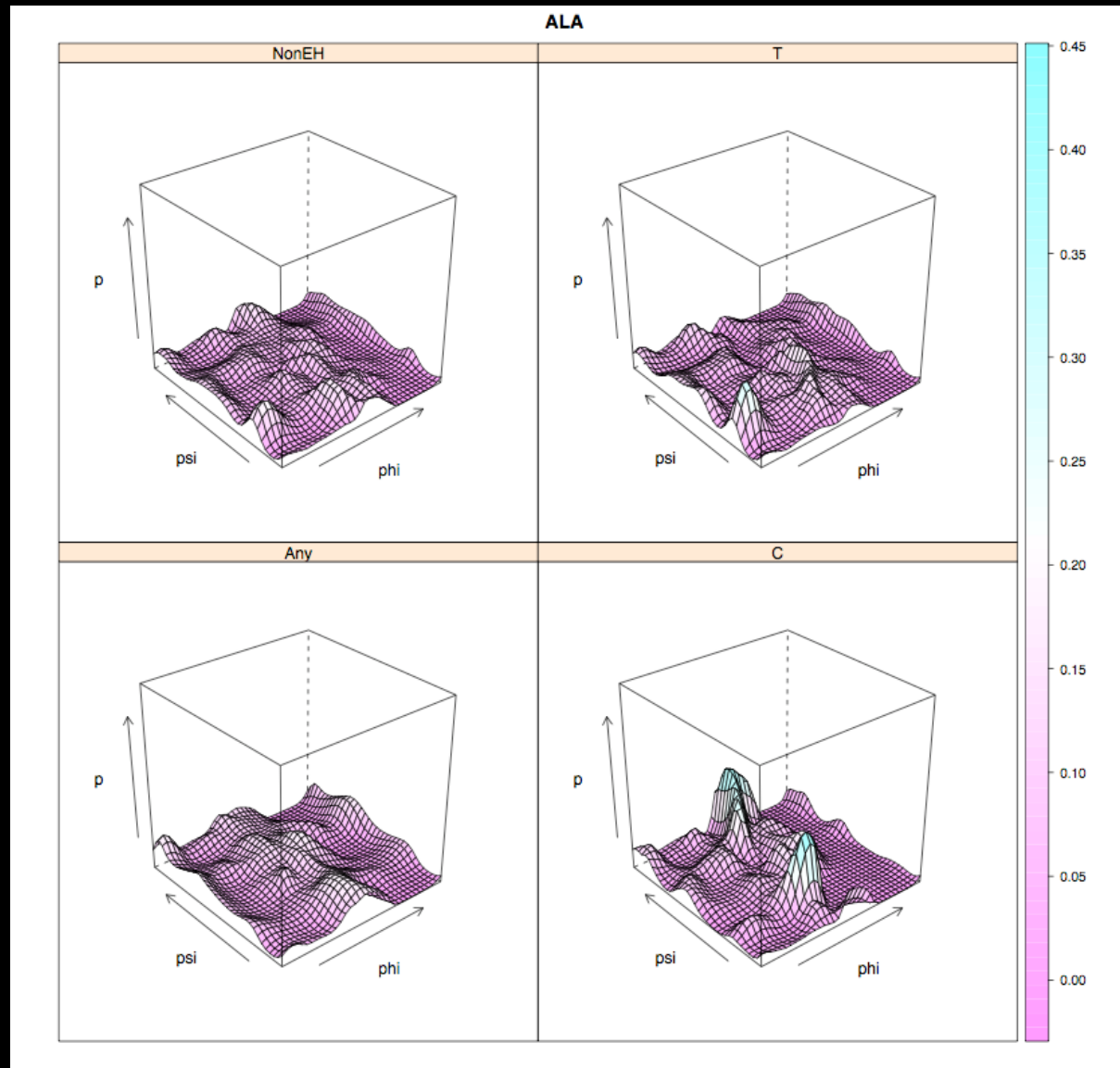
Glycine



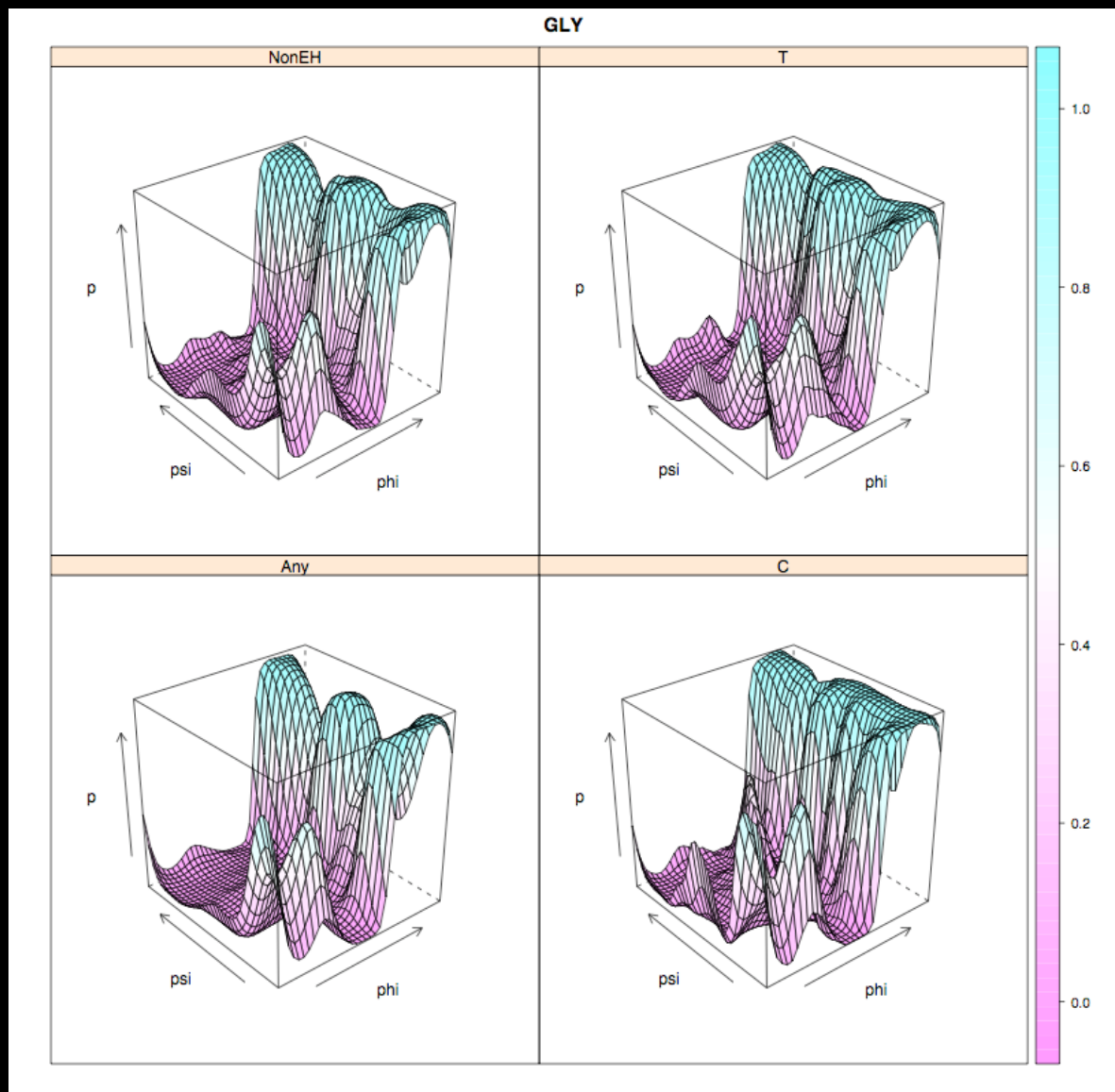
Proline



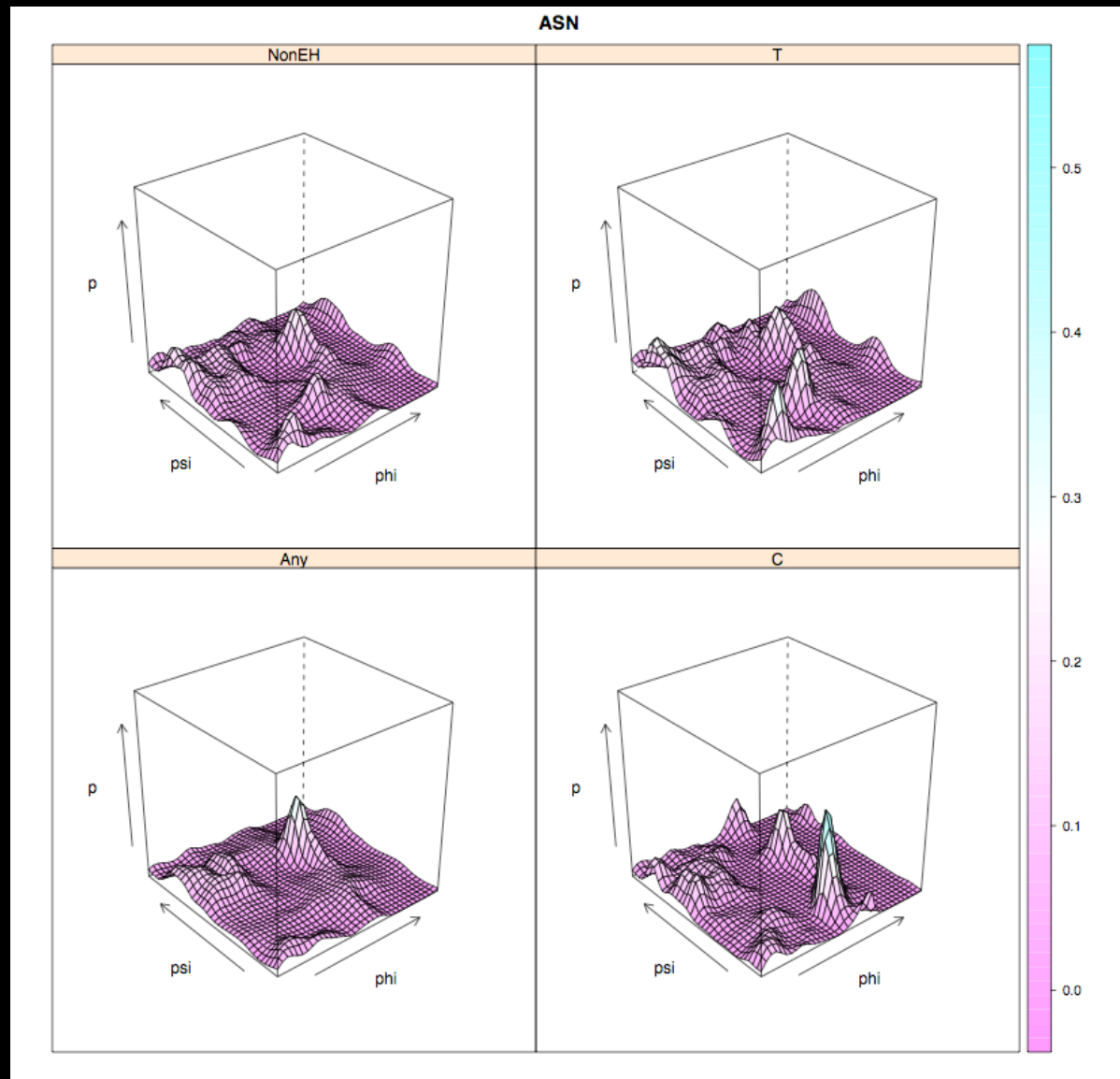
Propensity: Input set -- ALA



Propensity: Input set -- GLY



Propensity: Input set -- ASN



Acknowledgments

Maxim Shapovalov
Guoli Wang

NIH P20 GM76222-04

NIH R01 GM73784-04

NIH R01 GM84453-07

For Today's Graduate, Just One Word: Statistics

By [STEVE LOHR](#)

Published: August 5, 2009

MOUNTAIN VIEW, Calif. — At Harvard, Carrie Grimes majored in anthropology and archaeology and ventured to places like Honduras, where she studied Mayan settlement patterns by mapping where artifacts were found. But she was drawn to what she calls “all the computer and math stuff” that was part of the job.

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